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Candidate surname

Other names

Centre Number

Candidate Number

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Pearson Edexcel Level 3 GCE

Monday 26th June 2023

Afternoon (Time: 1 hour 30 minutes)

Paper
reference

9FM0/4C

Further Mathematics

Advanced

PAPER 4C: Further Mechanics 2

You must have:

Mathematical Formulae and Statistical Tables (Green), calculator

Total Marks

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear.
Answers without working may not gain full credit.
- Unless otherwise indicated, whenever a value of g is required, take $g = 9.8 \text{ m s}^{-2}$ and give your answer to either 2 significant figures or 3 significant figures.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 8 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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3. [In this question you may quote, without proof, the formula for the distance of the centre of mass of a uniform circular arc from its centre.]

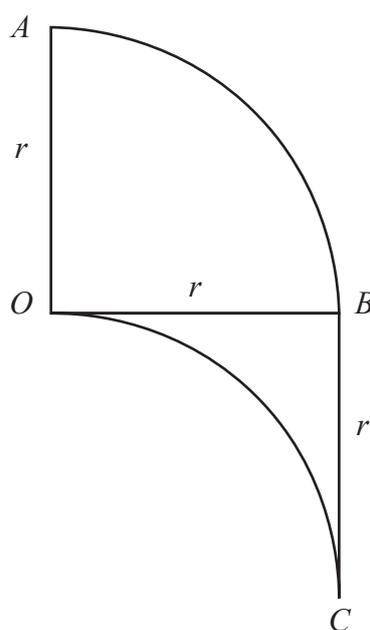


Figure 1

Five pieces of a uniform wire are joined together to form the rigid **framework** $OABCO$ shown in Figure 1, where

- OA , OB and BC are straight, with $OA = OB = BC = r$
- arc AB is one quarter of a circle with centre O and radius r
- arc OC is one quarter of a circle of radius r
- all five pieces of wire lie in the same plane

- (a) Show that the centre of mass of arc AB is a distance $\frac{2r}{\pi}$ from OA . (2)

Given that the distance of the centre of mass of the framework from OA is d ,

- (b) show that $d = \frac{7r}{2(3 + \pi)}$ (4)

The framework is freely pivoted at A .

The framework is held in equilibrium, with AO vertical, by a horizontal force of magnitude F which is applied to the framework at C .

Given that the weight of the framework is W

- (c) find F in terms of W (3)



6.

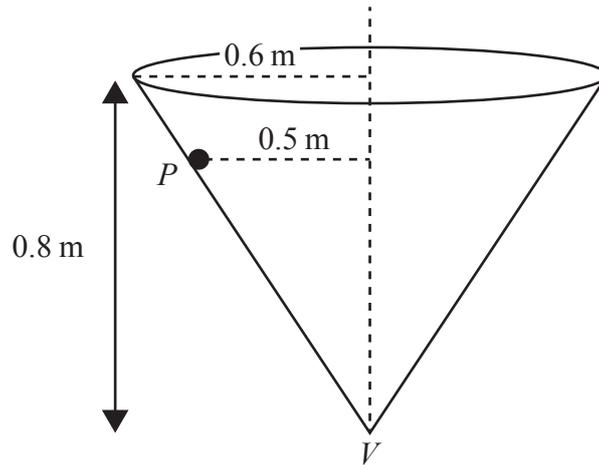


Figure 4

A hollow right circular cone, of internal base radius 0.6 m and height 0.8 m , is fixed with its axis vertical and its vertex V pointing downwards, as shown in Figure 4.

A particle P of mass $m\text{ kg}$ moves in a horizontal circle of radius 0.5 m on the rough inner surface of the cone.

The particle P moves with constant angular speed $\omega\text{ rad s}^{-1}$

The coefficient of friction between the particle P and the inner surface of the cone is 0.25

Find the greatest possible value of ω

(9)

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7.

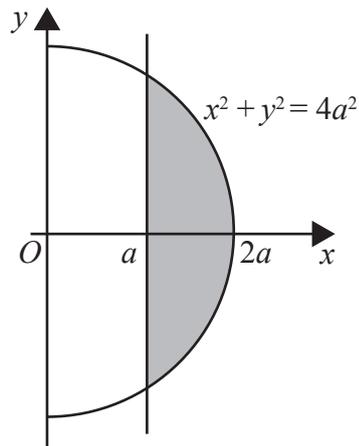


Figure 5

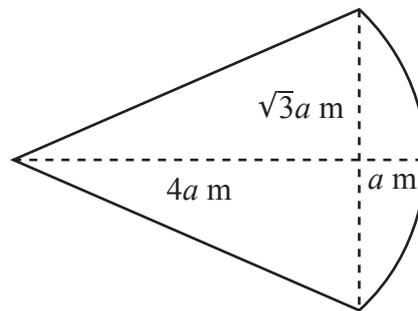


Figure 6

The shaded region shown in Figure 5 is bounded by the line with equation $x = a$ and the curve with equation $x^2 + y^2 = 4a^2$

This shaded region is rotated through 180° about the x -axis to form a solid of revolution.

This solid is used to model a dome with height a metres and base radius $\sqrt{3}a$ metres.

The dome is modelled as being non-uniform with the mass per unit volume of the dome at the point (x, y, z) equal to $\frac{\lambda}{x^2}$ kg m^{-3} , where $a \leq x \leq 2a$ and λ is a constant.

- (a) Show that the distance of the centre of mass of the dome from the centre of its plane face is $\left(4 \ln 2 - \frac{5}{2}\right)a$ metres.

(6)

A solid uniform right circular cone has base radius $\sqrt{3}a$ metres and perpendicular height $4a$ metres. A toy is formed by attaching the plane surface of the dome to the plane surface of the cone, as shown in Figure 6.

The weight of the cone is kW and the weight of the dome is $2W$

The centre of mass of the toy is a distance d metres from the plane face of the dome.

- (b) Show that $d = \frac{|k + 5 - 8 \ln 2|}{2 + k}a$

(4)

The toy is suspended from a point on the circumference of the plane face of the dome and hangs freely in equilibrium with the plane face of the dome at an angle α to the downward vertical.

Given that $\tan \alpha = \frac{1}{2\sqrt{3}}$

- (c) find the exact value of k .

(3)



